This talk aims at giving a more detailed description of the methods used to determine the fixed points of smoothing transforms.The fixed-point equation of the smoothing transform naturally leads to a functional equation for Fourier or Laplace transforms. One of the key steps in solving the functional equation for Fourier and Laplace transforms is to solve it for arbitrary decreasing functions first. We will present the key ideas how to solve this functional equation.